NUMERICAL PROBLEMS

P.4.1 A man pushos a lawn mover with a 40 N force directed at an angle of 20° downward from the horizontal. Find the work done by the man as he cuts a strip of grass 20 m long.

DATA. F = 40 N 0 = 20° d = 20 m

Sol: Using;  $W = F.d = Fd \cos \theta$ 

 $W = 40 \text{ N} \times 20 \text{ m} \times 60520$   $= 7.5 \times 10^{2} \text{ J}$   $= 1 \text{ N} \times \text{m} = 1 \text{ J}$   $= 1 \text{ P.4.2} \text{ A rain drop } (m = 3.35 \times 10^{5} \text{ kg}) \text{ falls vertically at a}$ constant speed under the influence of the forces of gravity and friction. In falling through 100m, how much work is done by (a) gravity and (b) friction.

DATA . m = 3.35 x 10 Kg Height = h = 100 m

- (a) Workdone due to gravity = ?
- (b) Work done due to friction = ?

Sol: We have

Work done due to gravity = W = meh  $W = 100 \text{ m} \times 9.8 \text{ m} 5^2 \times 3.35 \times 10^5 \text{ kg}^2$  = 0.0328 J

Work done due to both gravity and friction is the same. Here, the frictional force is acting on the rain drop against the gravitational force.so work done by friction = - 09328 J

## Chapter 04:Work and Energy

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P.4.3 Ten bricks, each 6 cm thick and mass 1-5 kg, lie flat on a table. How much work is required to stack them one on the top of another?

DATA. Mass of each brick = 1.5 Kg = m Thickness of brick = h = 6 cm = 0.06m work required to stack them one on the

top of another = W = ?

Sol: There is no work done for the Ist brick . We have to put bricks on it one by one. Therefore, every brick gets Some P.E w.r.t its height. so W = 0 + mgh + 2mgh + 3mgh + 4mgh + 5mgh + 6mgh + 7mgh + 8mgh + 9mgh W = 45mgh - 1Putting values, we have W = 45x1-5:09 x9-8m3x0.06m = 39.69 J = 40 J

	10	mg (9h)
	٩	1
	8	<b>.</b> 1
	7	1
	6	j
	2	i
	4	mg (3h)
	3	mg (3h) mg (2h)
1	2	mgh
4	1	٥.
W #		

P.4.4 An object of mass 6kg is travelling at a velocity of 5m 5'. What is its K.E? What will be its K.E if its velocity is double?

DATA. Mass of the object = m = 6 kg
velocity of " = V = 5 ms

(a) K.E = ? (b) K.E = ? (When its velocity is double)

Sol: (a) We know that

 $K = \frac{1}{2} m v^2$  $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \text{ kg} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times 6 \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times (5 \text{ ms}^{-1})$   $= \frac{1}{2} \times (5 \text{ ms}^{-1})$ 

(b) Now V= 10 ms, therefore  $|X.E| = \frac{1}{2}mv^{2}$   $= \frac{1}{2} \times 6 \times 8 \times (10 \text{ m/s}^{-1})$   $= 300 \text{ J} = 3.0 \times 10 \text{ J}$ 

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P.4.5 An electron strikes the screen of a cathode\_ray tube with a velocity of 1.0 × 10 ms. Calculate its K.E. The mass of an electron is 9.1 × 10 1 kg.

DATA. Velocity of electron = V = 1.0 × 10 ms Mass of electron = m = 9.1 x 1031 kg. K.E = ? Sol: As we know that; K.E = 1 my2 into a tank, 10 m higher than the reservoir, in 20 minutes. If density of water is 1000 kg m3 find (a) the increase in P.E (b) the power delivered by the pump. DATA. Volume of water = V = 100 m3 Height = h = 10 m Time taken = t = 20 min = 20 +6.5 = 12005 Density of water = 9 = 1000 kg m3. (d) Increase in P.E=? (b) Power delivered by the Pump = P=? Sol. As Density (8) = Mass (m)
Volume (V)  $m = V * \int \frac{1}{m} = 1000 \text{ Kg m}^{-3}$   $m = 10 \text{ Kg} \frac{1}{m} = 2$ workdone = P. E = mgh

Therease in P.E =  $9.8 \times 10^{5}$  (b) Now Power (P) =  $\frac{\text{Work}(W)}{\text{time}(t)}$ P= 9.8×16J = 8166.6 Watt P= 8.167×10 watt= 8.2KW

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P.4.7 A force (thrust) of 400N is required to overcome road friction and air resistance in propelling an automobile at 80 km h. What power (KW) must the engine develop?

DATA. F = 400 N Velocity = V = 80 km h = 80 × 1000 = 22.22 ms Power = P (in kw) =?

Sol: As P= F.V = FV coso = FV (: Force & Vel P= 400 N x 22.22 ms the same P= 8888 watt direction) = 8.9 x 10 K. Watt = 8.9 KW

P.4.8 How large a force is required to accelerate an electron (m=9.1×10 1kg) from rest to a speed of 2×10 ms through a distance of 5cm?

DATA. Mass of electron =  $m = 9.1 \times 10^{-31}$  kg

Initial velocity =  $V_i = 0$ Final "= $V_f = 2 \times 10^7 \text{ ms}^2$ Distance = d = 5 cm = 0.05 mForce required = F = ?

Sol: Using work-energy principle;  $F \times d = \frac{1}{2} \times mV_f^2 - \frac{1}{2} mV_i^2$ Putting the values, we have;  $F \times 0.05 \text{ in} = \frac{1}{2} \times 9.1 \times 10^{-31} \text{ kg} \times (2 \times 10^{-31} \text{ ms}^2) = 0$   $F = 3.6 \times 10^{-15} \text{ N}$   $F = 3.6 \times 10^{-15} \text{ N}$ 

P.4.9 A diver weighing 750 N drops from a board 10 m above the surface of a pool of water. Use the conservation of mechanical energy to find his speed at a point 5 m above the water surface, neglecting air friction?

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speed of diver = v = ?

sol. As we know;

Loss of P.E = Gain in K.E  $m_e(h_1 - h_2) = \frac{1}{2} \times m_1 \sqrt{2}$ V= 29(h, -h2)

Putting values, we have;

$$V = \sqrt{2 \times 9.8 \text{ m/s}^2 \times (10 \text{ m} - 5 \text{ m})}$$

$$V = \sqrt{9.9 \text{ m/s}^2} - \sqrt{2}$$

P.4.10 A child starts from rest at the top of a slide of height 4 m (a) What is his speed at the bottom if the slide is frictionless? (b) if he reaches the bottom with a speed of 6 m 3' what percentage of his total? energy at the top of the slide is lost as a result of friction?

DATA. Height of Slide = h = Am

(a) speed at the bottom = V = ?

(b) % age of total energy lost = ? (if V = 6ms)

Sol: (a) As Loss of P.E = Gain in K.E